

# Enhancing LQR and LQT Control Strategies for the Output Performance of PG36M555 DC Motors

Akhmad Azhar Firdaus<sup>1</sup>, Anggara Trisna Nugraha<sup>2</sup>, Rama Arya Sobhita<sup>2</sup>, Dhadys Ayu J. A.<sup>3</sup>

<sup>1</sup>Bio-Industrial Mechatronics Engineering, National Chung Hsing University, TAIWAN

<sup>2</sup>Marine Electrical Engineering, Shipbuilding Institute of Polytechnic Surabaya, INDONESIA

<sup>3</sup>Design and Manufacture Engineering, Shipbuilding Institute of Polytechnic Surabaya, INDONESIA

---

Article Info	Abstract
<p><b>Article history:</b></p> <p>Received 03 August, 2025</p> <p>Revised 15 October, 2025</p> <p>Accepted 01 November, 2025</p>	<p>A DC motor is commonly utilized as an actuator due to its ability to produce high torque. Controlling the motor's speed is one of the primary methods to manage its performance. Among various wireless communication options, radio waves are preferred since they do not require a clear line of sight between the transmitter and receiver. Employing multiple antennas offers benefits such as enhanced reliability and increased data transmission rates. This study focuses on designing and simulating four types of systems: SISO, SIMO, MISO, and MIMO. The performance of these configurations is evaluated and compared using Signal-to-Noise Ratio (SNR) and channel capacity, with variations in antenna count. Simulations were carried out in MATLAB to analyze how different antenna quantities (4, 8, and 16) affect channel capacity across an SNR range of 0 to 30 dB. The simulation outcomes reveal a substantial rise in system capacity, reaching up to 214 bits/Hz/sec when a 16x16 MIMO setup is applied at 30 dB SNR.</p> <p><b>Keyword:</b> Matlab, LRT, LQT, Performance, DC Motor, PG36M555</p>

---

**\*Corresponding Author:**

Name: Anggara Trisna Nugraha  
Email: [anggaranugraha@ppns.ac.id](mailto:anggaranugraha@ppns.ac.id)

---

## 1. Introduction

Direct Current (DC) motors remain one of the most widely utilized actuators in industrial and engineering applications due to their simple structure, high starting torque, ease of speed control, and reliable dynamic response. They are commonly deployed in robotics, manufacturing automation, transportation systems, and small-scale electromechanical devices where precise motion control is required. Despite these advantages, achieving high-performance operation in DC motor systems requires appropriate control strategies to ensure stability, fast transient response, minimal steady-state error, and robustness against disturbances. Without proper control optimization, DC motors may exhibit slow response, steady-state deviation, or sensitivity to parameter variations and external

noise. Consequently, the development of efficient control methods for DC motor systems remains a significant research topic in modern control engineering [1] [2] [3].

In contemporary industrial environments, automated control systems are increasingly implemented to improve operational efficiency, productivity, and reliability. Automated systems allow machines to execute predefined tasks accurately with minimal human intervention, reducing operational errors while increasing consistency and repeatability. In both large-scale industries and emerging mid-level enterprises, automation plays a crucial role in maintaining competitiveness and reducing production costs. The integration of intelligent control algorithms into actuator systems such as DC motors is therefore essential to meet the growing demand for high precision and fast response in automated processes [4] [5].

One of the central challenges in modern control engineering is the design of optimal controllers capable of delivering superior dynamic performance under physical and operational constraints. Optimal control theory provides a systematic framework for determining control inputs that minimize a predefined performance index while satisfying system dynamics. Instead of relying solely on heuristic tuning, optimal control methods mathematically formulate the control objective in terms of state variables and control effort, enabling a balanced trade-off between performance and energy consumption. The primary goal is to reduce deviations from the desired reference signal while maintaining system stability and minimizing control energy [6] [7].

Among the various optimal control techniques, the Linear Quadratic Regulator (LQR) has emerged as one of the most effective state-space-based methods for linear dynamic systems. LQR determines the optimal feedback gain matrix by minimizing a quadratic performance index composed of weighted state and control variables. The selection of weighting matrices  $Q$  and  $R$  plays a crucial role in shaping the system response, as these matrices define the relative importance of state error and control effort. Proper tuning of  $Q$  and  $R$  enables designers to achieve fast settling time, reduced overshoot, and improved steady-state accuracy. Due to its mathematical rigor and systematic formulation, LQR has been successfully applied in numerous engineering domains, including induction motor speed regulation, power system frequency control, aerospace stabilization systems, and robotic motion control [8] [9].

In addition to LQR, the Linear Quadratic Tracker (LQT) extends the optimal control concept by incorporating reference tracking capabilities. While LQR focuses primarily on state regulation toward zero, LQT introduces an additional feedforward term to enable accurate tracking of time-varying reference signals. This feature makes LQT particularly suitable for applications where maintaining precise speed or position trajectories is critical. By combining state feedback and feedforward compensation, LQT enhances tracking performance while preserving the optimality framework derived from quadratic cost minimization [10] [11] [12]. Although optimal control techniques such as LQR and LQT have been extensively studied in theoretical contexts, their practical performance must be evaluated through modeling and simulation before real-world implementation. Mathematical modeling of the DC motor is therefore a fundamental step in control system design. By representing the motor dynamics using differential equations and state-space formulations, it becomes possible to analyze system behavior under various control strategies. First-order modeling is often employed for simplified representation of speed dynamics, allowing clear observation of transient and steady-state characteristics. Simulation environments such as MATLAB/Simulink provide a flexible platform for implementing these models and evaluating controller performance under controlled scenarios, including the presence of disturbances or measurement noise [13] [14] [15] [16].

Despite the established advantages of optimal control methods, challenges remain regarding robustness against noise and parameter uncertainty. In practical systems, external disturbances,



## 2.1. First Order Mathematical Modeling

Mathematical modeling is done to obtain the response results of the DC motor. The mathematical model of the first-order system can be written as the following equation

$$\frac{C(s)}{R(s)} = \frac{K}{\tau s + 1} \quad (1)$$

$$K = \frac{\tau}{i} \quad (2)$$

Description:

$\tau$  = Torque

$i$  = Ampere

So the calculation on the DC motor DC Motor PG36M555 based on the specifications from the datasheet obtained is:

$$K = \frac{\tau}{i} = \frac{0.2}{2.1} = 0,095 \quad (3)$$

Substitute the results of equation 3 into equation 1 to obtain the mathematical model of the PG36M555 DC Motor.

$$G(s) = \frac{K}{\tau s + 1} = \frac{0,174}{0.687s + 1} \quad (4)$$

## 2.2. Linear Quadratic Regulator (LQR)

Linear Quadratic Regulator (LQR) is a method used in modern control theory [19]. Analysis of such systems is done using the state space approach. Due to the simple approach of the state space method, multi-input multi-output systems use this method. The state space equation for the system is generally written as:

$$\dot{X} = AX + Bu \quad (5)$$

In principle, the LQR method searches for a control signal  $u$  that minimizes the performance index  $J$ .

$$J = \int (X^T Q_x + u^T R_a) dt \quad (6)$$

LQR finds the optimal control input law  $u^*$ . The constraints imposed by the  $Q$  and  $R$  matrices minimize the performance index. The closed-loop optimal control law is defined as:

$$u^* = -Kx \quad (7)$$

Here,  $K$  represents the optimal feedback gain matrix, which functions to minimize the performance index of the system. This gain matrix plays a key role in determining the appropriate placement of the closed-loop poles to achieve optimal system behavior. The value of  $K$  is influenced by the system matrices  $A$  and  $B$ , as well as the weighting matrices  $Q$  and  $R$  [20]. To calculate the feedback gain  $K$ , the Algebraic Riccati Equation (ARE) must be solved. The solution to this equation

yields P, a symmetric and positive definite matrix. This matrix P is essential in defining the optimal control law and directly impacts the computation of the gain matrix K.

$$A^T P + PA - PBR^{-1}B^T P + Q = 0 \tag{8}$$

$$K = AX - BKx = (A - BK)x \tag{9}$$

Equation (8) and (9) become:

$$\dot{x} = AX - BKx = (A - BK)x \tag{10}$$

The block diagram showing the LQR configuration is shown in Figure 2.

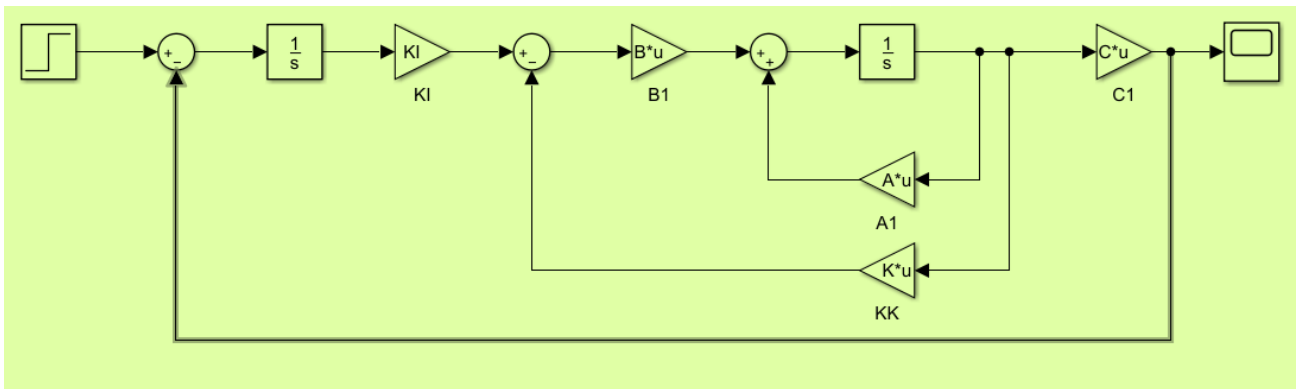


Figure 2. LQR Diagram Block

## 2.2. Linear Quadratic Tracker (LQT)

The LQT consists of the usual state feedback of a linear dynamic system together with an additional feed-forward control term. The feed-forward control term depends on the reference signal vector,  $r(t)$ . The vector  $r(t)$  is given by:

$$r(t) = [V_{ref}(t) \ 0]^T \tag{11}$$

Where,  $V_{ref}$  is a time-varying reference voltage signal. The LQT scheme minimizes the squared performance index to produce the optimal control decision which can be formulated in the following equation.

$$J = \frac{1}{2} \int_0^T [(x(t) - r(t))^T Q (x(t) - r(t)) + d(t)^T R d(t)] dt \tag{12}$$

Where, Q and R are the intermediate state and control weighting matrices, respectively. They are chosen such that;  $Q = Q^T \geq 0$  and  $R = R^T > 0$ . Due to the quadratic nature of the cost function, the control signal is proportional to the quadratic variation of the equation. Thus, if the state-variations are large; minimization and, hence, the convergence rate is faster.

$$d(t) = -Kx(t) + K_{ff}v_{ref}(t) \tag{13}$$

Where,

$$K = R^{-1}B^T P \tag{14}$$

$$K_{ff} = R^{-1}B^T((A - BK)^T)^{-1}H^TQ \quad (15)$$

The gain vector, K, helps to relocate the system poles to synthesize the optimal controller. The optimal gain vector depends on the symmetric positive definite matrix, P, shown in (14). The matrix, P, for a given system can be obtained by solving the Riccati Algebra Equation, shown in.

$$A^TP + PA - PBR^{-1}B^TP + H^TQH = 0 \quad (16)$$

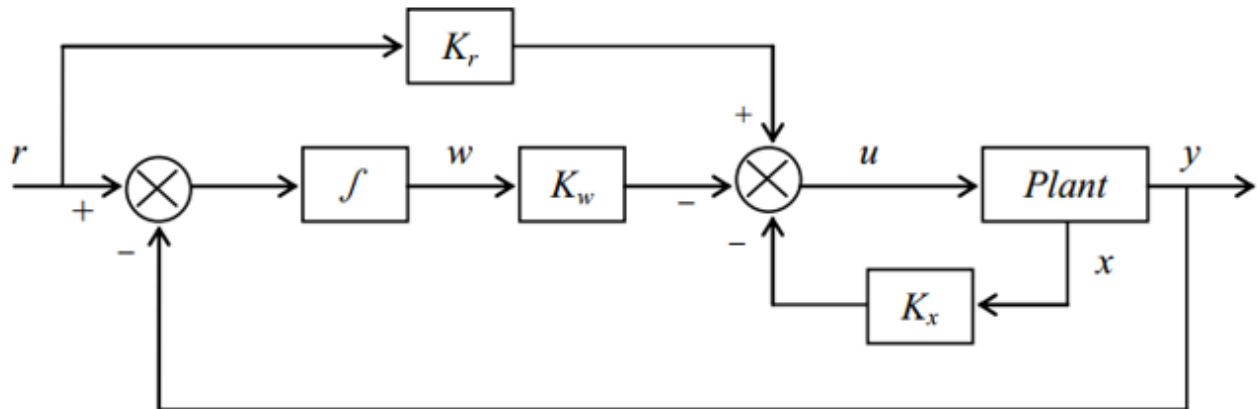


Figure 3. LQT Diagram Block

### 2.3. Block diagram first order DC Motor PG36M555

In the first order motor block diagram, the aim is to find out the original response results of the DC motor if the PG36M555 DC Motor is not added to the method carried out in the Simulink software.

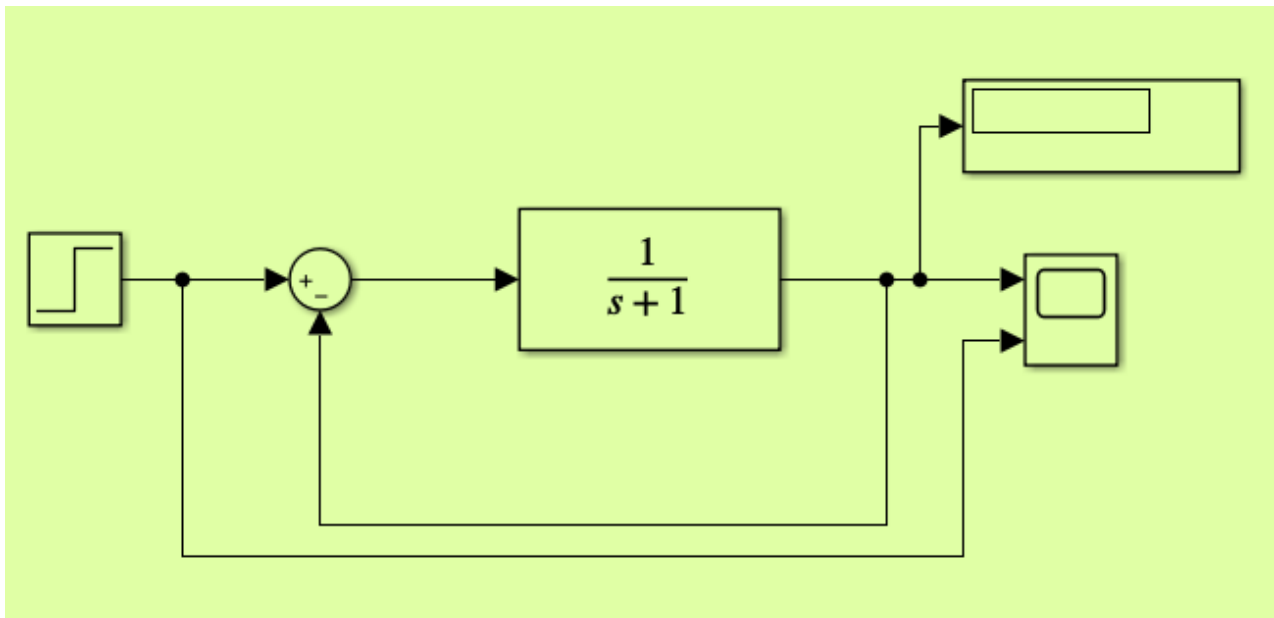


Figure 4. Block diagram first order in Simulink

Figure 4 shows a first-order block diagram of a DC motor consisting of an input and an output. The input used is a step response type. The transfer function in the diagram can contain a first-order DC motor modeling. The response results will be displayed on the scope and display to find out the maximum response value produced.

## 2.4. Block diagram LQR DC Motor PG36M555

In the LQR block diagram of the PG36M555 DC Motor, the aim is to find out the response results of the DC motor if the DC motor is given the addition of the LQR optimization method which is carried out on the Simulink software.

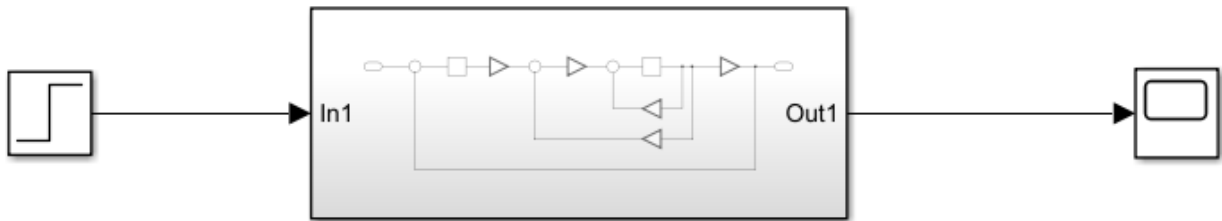


Figure 5. Block diagram LQR Motor in Simulink



Figure 6. Block diagram LQR Motor in Simulink with noise

## 2.5. Block diagram LQT DC Motor PG36M555

In the LQT block diagram of the PG36M555 DC Motor, the aim is to find out the response results of the DC motor if the DC motor is given the addition of the LQT optimization method which is carried out on the Simulink software.

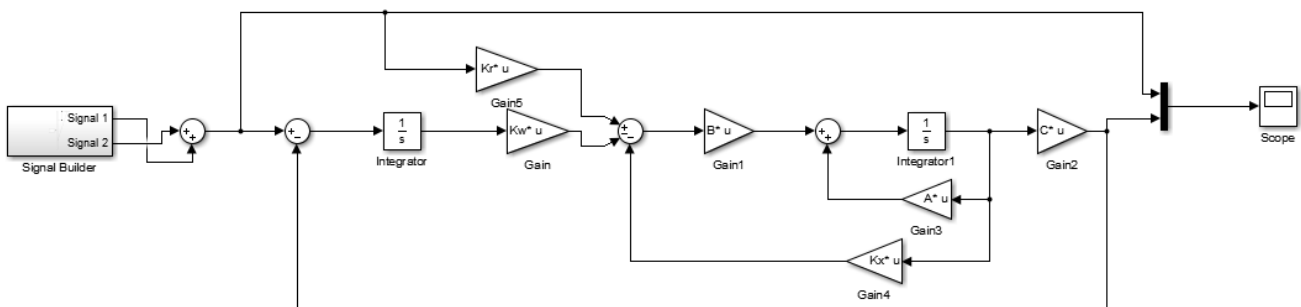
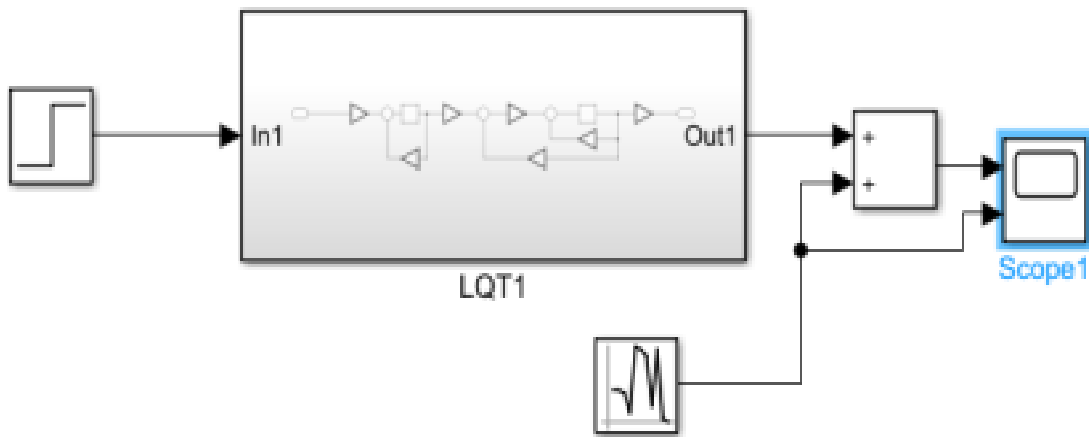


Figure 7. Block diagram LQT Motor in Simulink

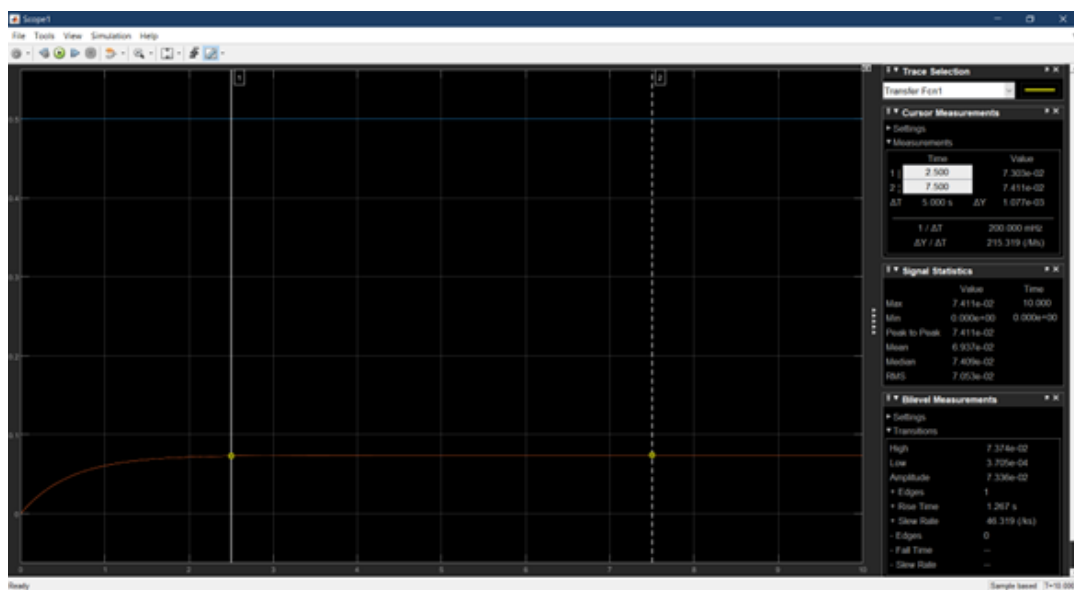


**Figure 8.** Block diagram LQR Motor in Simulink with noise

### 3. Results And Discussion

This section discusses the results of the PG36M555 DC motor response in the first-order mathematical model and when given the LQR method with and without noise. The response results are obtained using simulations in the Simulink Matlab software.

#### 3.1. First Order Response Results of PG36M555 DC Motor



**Figure 9.** Response Results of PG36M555 DC Motor

In the output response of the first-order modeling shown in Figure 9, the motor's response appears to deviate significantly from the desired setpoint. The orange waveform represents the actual motor response, while the blue line indicates the target setpoint. The intended value is 0.5, yet the motor only reaches approximately 0.07. The observed PG36M555 DC motor demonstrates linear behavior, as indicated by the absence of ripples in the signal. The system reaches a steady state around the 2-second mark after being powered on. However, the overall response is considered relatively slow [10] [14] [15].

### 3.2. PG36M555 DC Motor Response Results Using LQR Method

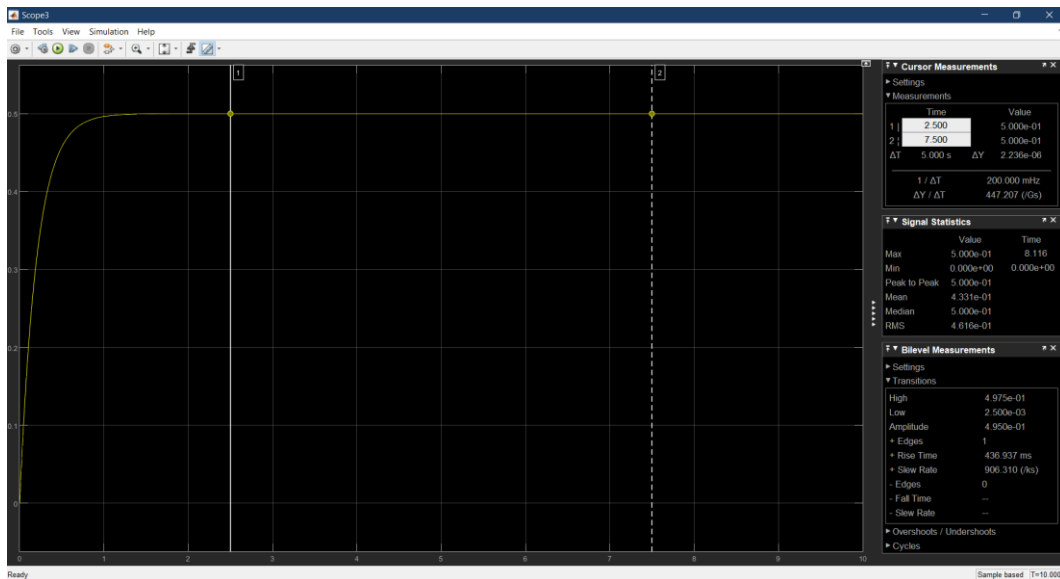


Figure 10. DC Motor Response Results Using LQR Method

In the output response shown in Figure 10, the PG36M555 DC motor demonstrates a significantly improved performance when the LQR method is applied. The response curve aligns precisely with the desired setpoint value of 0.5. The motor successfully reaches the setpoint at approximately 1.2 seconds without experiencing any overshoot or undershoot. This indicates that applying the LQR control method leads to a much more accurate and stable response compared to the system without LQR implementation [2] [3] [11].

### 3.3. Comparison Results of DC Motor Response Using LQR

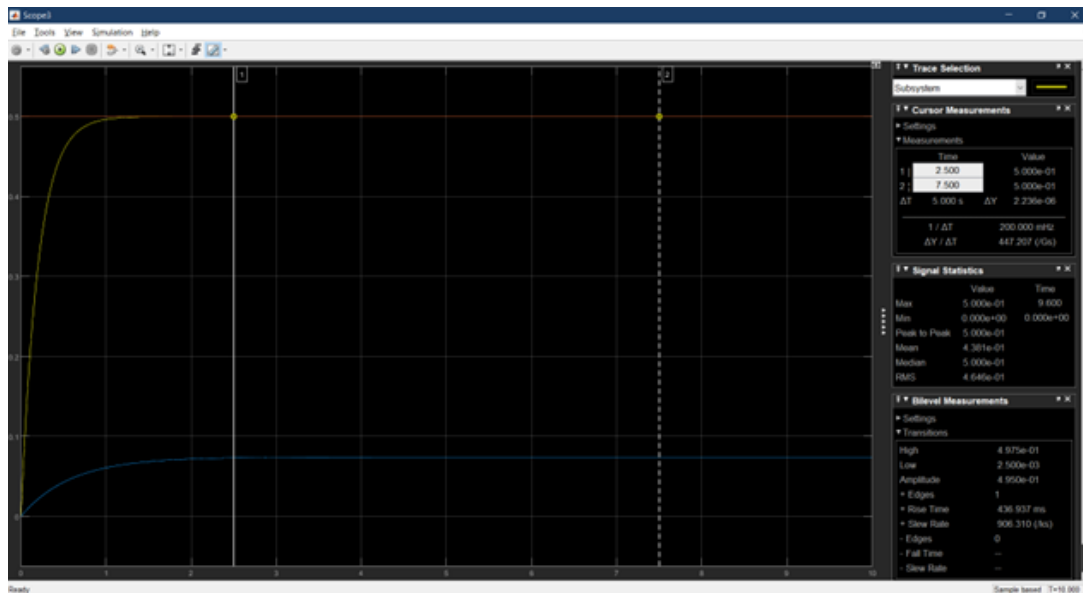


Figure 11. Comparison Results of DC Motor Response Using LQR Method and Without Method

In the comparison output response shown in Figure 11, the PG36M555 DC motor displays noticeably different behaviors when controlled with and without the LQR method. The orange

waveform represents the desired setpoint, the blue curve shows the motor's response without LQR, and the yellow curve indicates the response with LQR applied. As clearly illustrated in the figure, the motor response under LQR control outperforms the response without it. Not only does the LQR-controlled system closely follow the setpoint without any overshoot or undershoot, but it also reaches steady-state significantly faster, highlighting the improved performance and stability brought by the LQR approach [16] [17] [18].

### 3.4. PG36M555 DC Motor Response Using LQR Method with Noise

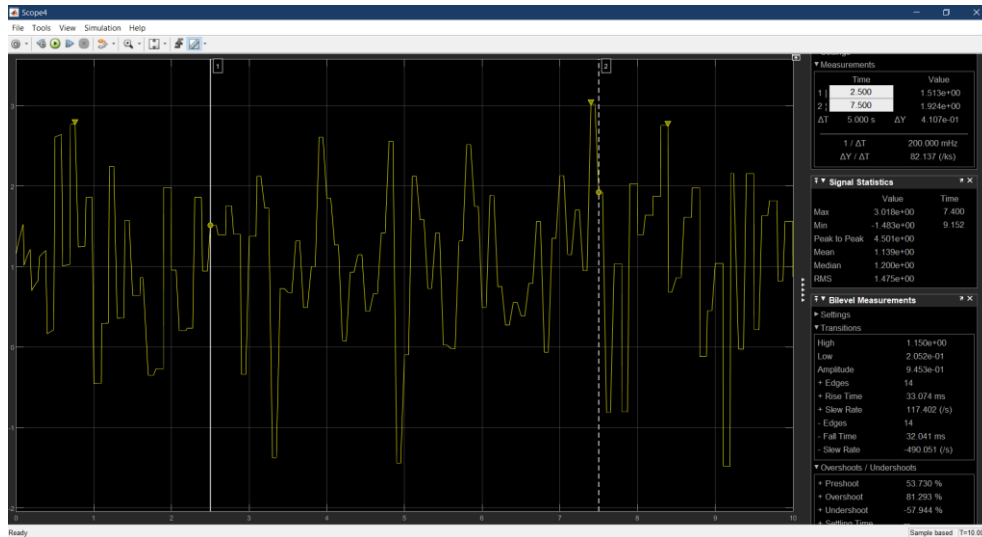


Figure 12. DC Motor Response Results Using LQR Method with Noise

Based on the results shown in Figure 12, the yellow signal representing the response of the PG36M555 DC motor under LQR control undergoes a noticeable change in shape after noise is introduced. The signal becomes highly distorted, displaying significant ripples and closely mimicking the characteristics of the injected noise. As a result, the motor response loses its linearity and deviates significantly from a stable steady-state condition at the intended setpoint [1] [2].

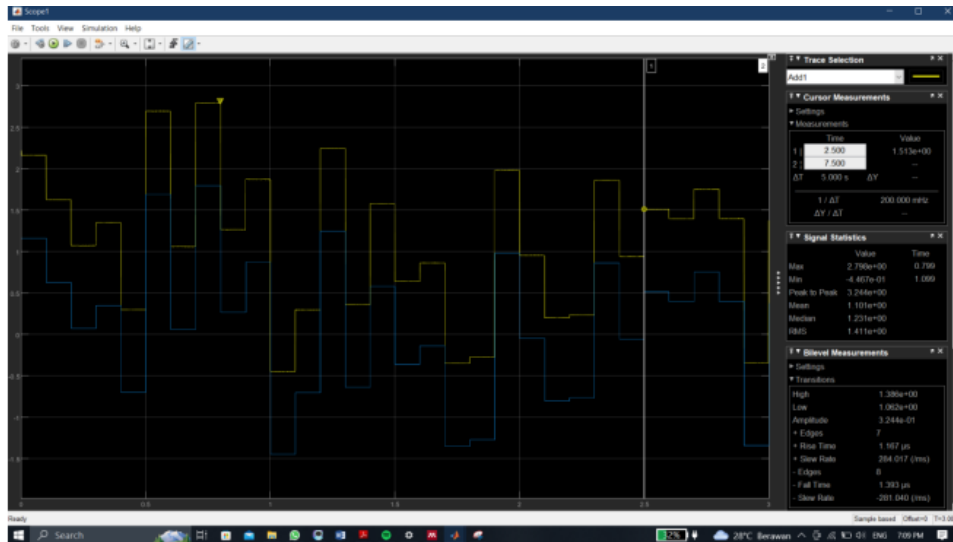
### 3.5. PG36M555 DC Motor Response Results Using LQT Method



Figure 13. DC Motor Response Results Using LQT Method

In the output response modeling shown in the figure above, the PG36M555 DC motor controlled using the LQT method successfully reaches the desired setpoint of 0.5. The response time to reach steady state is exceptionally fast, recorded at just 8.36 microseconds. However, the response exhibits a 4.7% overshoot and a slight 0.8% undershoot, indicating minor deviations before stabilizing at the target value [4] [6].

### 3.6. Comparison Results of DC Motor Response



**Figure 14.** Comparison Results of DC Motor Response Using LQT Method and Without Method

As shown in Figure 14, the yellow signal representing the response of the PG36M555 DC motor using the LQT method undergoes a significant change in shape after noise is introduced. The signal becomes heavily distorted, exhibiting numerous ripples and closely following the pattern of the applied noise. Consequently, the response loses its linear characteristics and deviates substantially from a stable steady-state condition at the intended setpoint [13] [18].

### 3.7. PG36M555 DC Motor Response Using LQT Method with Noise



**Figure 15.** DC Motor Response Results Using LQT Method with Noise

In the comparative output response shown in Figure 15, the Maxon EC-I 40 70 Watt DC motor displays distinct differences in behavior when operated with and without the LQT control method. The orange waveform represents the desired setpoint, the blue curve illustrates the motor's response without LQT, and the yellow curve shows the response with LQT applied. From the figure, it is evident that the motor's performance with LQT is significantly better, demonstrating a response that more closely follows the setpoint and overall improved system behavior compared to operating without the LQT method.

## 4. Conclusion

This study presents a systematic modeling and simulation-based evaluation of optimal control strategies to enhance the dynamic performance of the PG36M555 DC motor. A first-order mathematical model was developed to characterize the motor dynamics, and its open-loop response was analyzed as a baseline reference. The uncontrolled system exhibited slow transient behavior and substantial steady-state deviation, reaching only approximately 0.07 of the intended 0.5 setpoint and requiring nearly 2 seconds to stabilize, thereby highlighting the necessity of control optimization. The application of the Linear Quadratic Regulator (LQR) significantly improved system performance, enabling accurate setpoint tracking without overshoot or undershoot and reducing the settling time to approximately 1.2 seconds, confirming the effectiveness of optimal state-feedback control in improving stability and precision. Furthermore, the Linear Quadratic Tracker (LQT) achieved even faster convergence, reaching steady state in approximately 8.36 microseconds, albeit with minor overshoot (4.7%) and undershoot (0.8%), demonstrating superior tracking capability under nominal conditions. However, robustness analysis under noise disturbances revealed that both LQR and LQT experienced performance degradation, with output signals becoming distorted and deviating from steady-state stability. These findings indicate that while optimal control strategies substantially enhance nominal dynamic response and tracking performance, their sensitivity to noise remains a practical limitation. Overall, this work provides a comprehensive comparative assessment of LQR and LQT implementations for commercial DC motor systems and offers practical insight into their advantages and constraints in real-world control applications.

## Acknowledgement

The authors would like to express their sincere appreciation to the Shipbuilding Institute of Polytechnic Surabaya for providing the academic environment and technical facilities necessary to conduct this research. Special thanks are extended to the Marine Electrical Engineering Laboratory for supporting the modeling and simulation activities using MATLAB/Simulink. The authors also acknowledge the valuable discussions and technical insights contributed by colleagues and research collaborators, which significantly enhanced the quality of this work. Finally, gratitude is conveyed to all institutional stakeholders whose support and encouragement made the completion of this study possible.

## References

- [1] Razi, M., Murgovski, N., McKelvey, T., & Wik, T. (2021). Design and comparative analyses of optimal feedback controllers for hybrid electric vehicles. *IEEE Transactions on Vehicular Technology*, 70(4), 2979-2993.
- [2] Xue, W., Fan, J., Lopez, V. G., Jiang, Y., Chai, T., & Lewis, F. L. (2020). Off-policy reinforcement learning for tracking in continuous-time systems on two time scales. *IEEE transactions on neural networks and learning systems*, 32(10), 4334-4346.

- [3] Magriza, Rania Yasmin, et al. "Design and Implementation of Water Quality Control in Catfish Farming Using Fuzzy Logic Method with IoT-Based Monitoring System." *Jurnal Teknologi Maritim* 4.1 (2021): 13-18.
- [4] Jamil, M. H., et al. "The existence of rice fields in Makassar City." *IOP Conference Series: Earth and Environmental Science*. Vol. 681. No. 1. IOP Publishing, 2021.
- [5] Paluga, Ary Pratama, et al. "Renewable Energy System Optimization: Mppt Inverter Integration, Energy Storage Systems, And Its Impact on Sustainability and Efficiency Use Of Energy." *MEIN: Journal of Mechanical, Electrical & Industrial Technology* 1.2 (2024): 12-17.
- [6] Nugraha, Anggara Trisna, et al. "Comparison of Insulated Switch Gear with Desiccant Addition to SF6 Gas Quality System at Waru Substation." *JEEMECS (Journal of Electrical Engineering, Mechatronic and Computer Science)* 6.2 (2023): 77-86.
- [7] Li, X., Luo, Y., Chen, W., & Huang, T. (2021). Improved PID control method and its application to DC motor speed regulation. *Journal of Electrical Engineering & Technology*, 16(2), 1099–1109.
- [8] Fauzi, Ahmad Raafi, et al. "Performance of Permanent Magnet Synchronous Generator (pmsg) 3 Phase Radial Flux Results Modification of Induction Motor." *MEIN: Journal of Mechanical, Electrical & Industrial Technology* 1.2 (2024): 5-11.
- [9] Sobhita, R. A. (2024, November). Differential Optimization Control for MG-16B DC Motor with LQR and LQT Circuits. In *Conference of Electrical, Marine and Its Application* (Vol. 3, No. 1, pp. 1-11).
- [10] Haj, Muhammad Izzul, Rama Arya Sobhita, and Anggara Trisna Nugraha. "Performance Analysis of DC Motor in SISO Circuit Using LQR Control Method: A Comparative Evaluation of Stability and Optimization." *ICCK Transactions on Power Electronics and Industrial Systems* 1.1 (2025): 23-30.
- [11] Jamil, M. H., et al. "The existence of rice fields in Makassar City." *IOP Conference Series: Earth and Environmental Science*. Vol. 681. No. 1. IOP Publishing, 2021.
- [12] Agna, Diego Ilham Yoga, Salsabila Ika Yuniza, and Anggara Trisna Nugraha. "The Single-Phase Controlled Half Wave Rectifier with Single-Phase Generator Circuit Model to Establish Stable DC Voltage Converter Result." *International Journal of Advanced Electrical and Computer Engineering* 3.3 (2022).
- [13] As'ad, Reza Fardiyah, Salsabila Ika Yuniza, and Anggara Trisna Nugraha. "The Effect of 3 Phase Full Wave Uncontrolled Rectifier on 3 Phase AC Motor." *International Journal of Advanced Electrical and Computer Engineering* 3.2 (2022).
- [14] Pambudi, Dwi Sasmita Aji, et al. "Main Engine Water Cooling Failure Monitoring and Detection on Ships using Interface Modbus Communication." *Applied Technology and Computing Science Journal* 4.2 (2021): 91-101.
- [15] Setiawan, Edy, et al. "Integration of Renewable Energy Sources in Maritime Operations." *Maritime Infrastructure for Energy Management and Emission Reduction Using Digital Transformation*. Singapore: Springer Nature Singapore, 2025. 185-210
- [16] Ali, M., et al. (2020). Adaptive PID control of DC motor using fuzzy logic. *IEEE Access*, 8, 137532–137541.
- [17] Vidhya, S., & Sundararajan, T. (2022). Comparison of Ziegler-Nichols and modified tuning for PID controller in DC motor control. *International Journal of Electrical and Computer Engineering (IJECE)*, 12(2), 1632–1640